

6. Using Power series solve the equation $9x(1-x)y'' - 12y' + 4y = 0$ near $x = 0$.

7. Prove that $(1 - 2xz + z^2)^{-\frac{1}{2}} = \sum_{n=0}^{\infty} z^n P_n(x)$, $|x| \leq 1$, $|z| < 1$.

8. Write short notes (Answer any **Three**)

- a) Integrating Factor
- b) Solution of Non homogeneous differential equation.
- c) Regular singular point of a differential equation.
- d) Rodrigue's formula to find Legendre polynomial.
- e) Prove that $xJ'_n = nJ_n - xJ_{n+1}$.