

# M.Sc. Applied Mathematics Syllabus (Two Years Programme)

# **School of Applied Sciences**

Centurion University of Technology & Management

# 2024-25

# M.Sc. (Mathematics) Syllabus Course Structure (Core Courses)

Sl.No	Code	Subject Name	Cerdit	<b>Course Type</b>
				(Th+Pr+Pj)
1	CUTM1525	Heat and Mass Transfer	4	2+1+1
2	CUTM1526	Numerical Methods for CFD	4	2+1+1
3	CUTM1527	Fluid Dynamics	4	3+0+1
4	CUTM2381	Grid Generation and CFD Simulation using Simulia	4	0+2+2
5	CUTM2378	Research Methodology & IPR	4	2+0+2
6	CUTM1530	Advanced differential equations	4	2+1+1
7	CUTM1531	Graph Theory	4	3+1+0
8	CUTM1532	Optimization techniques	4	3+1+0
9	CUTM1533	Advanced Statistical Methods	4	2+1+1
10	CUTM1534	Applied Number Theory	4	3+1+0
11	CUTM1535	Advanced complex analysis	4	3+0+1
12	CUTM1536	Topology	4	3+0+1
13	CUTM1537	Differential Geometry	4	3+0+1
14	CUTM1538	Advanced Algebra	4	3+0+1
15	CUTM1018	Data Analysis and Visualization using Python	4	0+1+3
16	CUTM1019	Machine Learning using Python	4	1+2+1
		Total	64	



# **CUTM1525 HEAT AND MASS TRANSFER**

Subject Name	Code	Type of course	T-P-Pj (Credit)	Prerequisite
HEAT AND MASS TRANSFER	CUTM1525	Theory + Practice + Project	2-1-1	Nil

# Objective

- To introduce basic mechanisms of heat and mass transfer under steady state and transient conditions.
- To establish mathematical equations for energy conservation in different geometries and configurations.
- To provide comprehensive study on different modes of heat and mass transfer.

# Course outcome

After completion of the course, students will be able to

COs	Course outcomes
CO1	explain fundamental concepts of heat transfer
CO2	apply heat conduction equations to different surface configurations under steady
	state and transient conditions and solve problems.
CO3	solve problems related to convective heat transfer
CO4	apply basic principles of radiation in radiative heat transfer between different types
	of surfaces to solve problems.
CO5	apply diffusive and convective mass transfer equations and correlations to solve
	problems for different applications.

# **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	1		3		2			2	2		3	3	2	2
CO2	3	2	2	2	2	2	1			2		1	2	1	3
CO3	3		1	2						2		2	1	3	3
<b>CO4</b>	2	2	2		2		3					3	3	2	3
CO5	1	1	2	1		1	1			1			2	2	2

# CUTM1525 Heat and Mass Transfer (2-1-1)

#### Module I (T-3 Hrs.+P-2Hrs.)

Introduction to heat transfer: Heat Transfer Mechanisms Conduction: Fourier's Law of Conduction, General Heat Conduction Equation in Different Coordinate Systems (No Derivation), One Dimensional Steady State Conduction in Plane Wall, Conduction with Internal Heat Generation.

**Practice 1**: To find the thermal conductivity of a material by the two slabs guarded hot plate method.

Assignment 1: Assignment on Conduction.

#### Module II (T-2 Hrs.+P-2Hrs.)

Fins and Transient Conduction:

Overall Heat Transfer Coefficients, Unsteady State Heat Conduction, Lumped Heat Capacity System and Lumped Capacitance Method.

**Practice 2:** To find the thermal resistance of the sample. **Assignment 2:** Assignment on Fins and Transient Conduction.

#### Module III (T-4 Hrs.+P-4Hrs.)

Convection:

Thermal Boundary Layer, Principles and Governing Equations, Forced Convection: External Flow over a Flat Plate, Internal Flow Through Pipe, Natural Convection: Vertical & Horizontal Surfaces.

**Practice 3**: To determine the overall heat transfer coefficient at the surface of a given vertical metal cylinder by the natural convection method.

Practice 4: To verify Newton's Law of Cooling of different materials and different liquids.

Assignment 3: Assignment on Convection.

#### Module IV (T-2 Hrs.+P-2Hrs.)

Heat Transfer with Phase Change:

Film Wise and Drop Wise Condensation, Boiling Heat Transfer, Regimes of Boiling.

# Module V (T-2 Hrs.+P-2Hrs.)

Heat Exchangers:

Types of Heat Exchangers, Heat Exchanger Analysis, LMTD, Overall Heat Transfer Coefficient, Heat Exchanger Effectiveness, NTU.

**Practice 5:** Determination of Effectiveness and Efficiency of Parallel Flow and Counter Flow Heat Exchanger.

Assignment 4: Assignment on Heat Exchangers.

# Module VI (T-4 Hrs.+P-2Hrs.)

Radiation:

Black Body Emission, Emissive Power, Laws of Radiation, Nature of Black Bodies, Radiation Shape Factor, Radiation Heat Transfer Between Two Surfaces.

**Practice 6:** To find the emissivity of different material surface.

Assignment 5: Assignment on Radiation.

# Module VII (T-3 Hrs.+P-2Hrs.)

Mass Transfer:

Introduction, Analogy between heat and mass transfer, Mass diffusion, Fick's law of diffusion, boundary conditions, Steady mass diffusion through a wall, Mass convection.

Assignment 6: Assignment on Mass Transfer.

#### **Text Books:**

- 1. Mahesh M. Rathore, Engineering Heat Transfer, Jones & Bartlett Learning, 2011
- 2. Yunus A. Cengel & Afshin J. Ghajar, "Heat and Mass Transfer-Fundamentals and Applications", McGraw Hill, 5th Edition 2015
- 3. Yunus Cengel, Heat And Mass Transfer: Fundamentals And Applications, McGraw- Hill Higher Education, 2014

#### **Reference Books:**

- 1. R.C Sachdeva, Fundamentals of Heat and Mass Transfer
- 2. R.K. Rajput, Heat Transfer, Laxmi Publication



# **CUTM1526 NUMERICAL METHODS FOR CFD**

Subject Name	Code	Type of course	T-P-Pj (Credit)	Prerequisite
NUMERICAL METHODS FOR CFD	CUTM1526	Theory + Practice + Project	2-1-1	Nil

# Objective

- To introduce basic concepts of computational fluid dynamics (CFD).
- To familiarize different numerical methods to deal with the problems of CFD.
- To facilitate computational tools for solving linear and non-linear partial differential equations related to fluid dynamics and heat transfer.

#### **Course outcome**

After completion of the course, students will be able to

COs	Course outcomes
CO1	explain basic concepts of CFD
CO2	classify the equations governing the CFD problems
CO3	demonstrate the principles of numerical analysis and concepts of consistency,
	stability, and convergence.
CO4	examine finite difference/volume schemes on model problems of computational fluid
	dynamics.
CO5	construct program-code using Python to obtain numerical solutions of partial
	differential equations, relevant to Computational Fluid Dynamics.

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	2		1	3	1	2	2			1		3	3	2	3
CO2	3	2		2	1		1			2	1	1	2	1	3
CO3	3	2	1	1		2				1		2	1	2	2
<b>CO4</b>	3		2		2		1				2	3	2	2	3
CO5		1		1		1	1		1	2		1	2	3	1

# **Course Outline** CUTM1526 Numerical Methods for CFD (2-1-1)

#### **MODULE I**

#### **Introduction to CFD**:

Basics of computational fluid dynamics, Definition and overview of CFD - need, advantages, problem areas, Governing equations of fluid dynamics – Continuity, Momentum and Energy equations, Non-Dimensional form of these governing equations, Classifications of PDE: Elliptic, Parabolic and Hyperbolic equations.

#### **MODULE II**

#### **Finite Difference Method (FDM):**

Derivation of Finite difference equations (FDE) of 1<sup>st</sup> and 2<sup>nd</sup> order derivatives using Taylor series expansion. Explicit method-FTCS Method, Implicit method-BTCS Method, Crank-Nicholson method, Error, Convergence and stability analysis of above numerical Scheme, Keller Box Method.

#### **MODULE III**

#### **Solution of Simultaneous Equations:**

Direct and Iterative methods; Gauss-elimination, Gauss-Jordan, Gauss-Jacobi and Gauss-Seidel methods, Tri Diagonal Matrix Algorithm (TDMA) (Thomas)

Practice 1: Gauss-elimination method using PythonPractice 2: Gauss-Seidel method using PythonPractice 3: Tri Diagonal Matrix Algorithm using Python

**Project 1:** Solution of Simultaneous Equations using Gauss-Jordan method. **Project 2:** Solution of Simultaneous Equations using Gauss-Jacobi method.

#### **MODULE IV**

#### **Application of FDM:**

Solutions of Elliptic PDE: One-and Two-dimensional steady heat conduction, Laplace's Equation, Poisson's equation, Parabolic PDE: Unsteady heat conduction, Stoke's 1<sup>st</sup>& 2<sup>nd</sup> Problems, Hyperbolic PDE: One-dimensional wave equation

Practice 4: Solution of One-dimensional steady heat conduction using Python.
Practice 5: Solution of Laplace's equation using Python.
Practice 6: Solution of Unsteady heat conduction using Python.
Practice 7: Solution of One-dimensional wave equation using Python.
Practice 8: Solution of Stoke's Problem.

**Project 3:** Solution of Poisson's equation. **Project 4:** Solution of Burger's equation.

# **MODULE V**

#### **Finite Volume Method (FVM):**

Fundamentals of FVM, Integral Form of 1-D Conservation equation, Finite Volume Method in 2-D

#### **MODULE VI**

#### **Application of FVM:**

Solutions of 1-D steady state Diffusion and Convection equations.

**Project 5:** Solutions of 1-D steady state Diffusion equation.

#### **MODULE VII**

#### **Application of FVM:**

Solutions of 2-D steady state Diffusion and Convection equations.

**Project 6:** Solutions of 2-D steady state Convection equation.

#### **Text Books:**

- 1. Computational Fluid dynamics by John D. Anderson, Jr
- 2. Computational Fluid dynamics and Heat Transfer, by John C. Tannehill , Dale A. Anderson , Richard H. Pletcher
- 3. Introduction to finite elements in engineering, by Tirupathi R. Chadraupala, Ashok D. Belegundu, Chapter 3.
- 4. An introduction to computational fluid dynamics, by H K Versteeg and W Malalasekera, Chapter 4,5



# CUTM1527 FLUID DYNAMICS

Subject Name	Code	Type of course	T-P-Pj (Credit)	Prerequisite
FLUID DYNAMICS	CUTM1527	Theory+Project	3-0-1	Nil

# Objective

- To introduce the foundations of fluid dynamics.
- To provide a clear view on governing equations of fluid dynamics.
- To work with different types of flows.

#### **Course outcome**

After completion of the course, students will be able to

COs	Course outcomes
CO1	recognize different types of flow
CO2	explain mass, momentum and energy conservation and their mathematical equations in
	different physical situations.
CO3	distinguish and analyze the governing equations of fluid dynamics in various
	formulations for compressible and incompressible, viscous and inviscid flows.
CO4	estimate the impact of different physical phenomena based on dimensional analysis
CO5	examine mathematical properties of governing equations and be able to critically
	evaluate correct boundary/initial value problems for various flows.

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1		1	1	3	1	2	2			1		3	3	3	2
CO2	1	2		2		1	1			2	1	1	2	1	3
CO3	3		2		1	2	2			1	1	2	1	1	3
CO4	2		2		2					2	2		2	3	2
CO5	2	1		1		1	1			2		1	2	1	1

#### \*High-3, Medium-2, Low-1

# Course Outline CUTM1527 Fluid Dynamics (3-0-1)

#### MODULE – I (4hr+0hr+2hr)

Kinematics of Fluids, Methods describing Fluid motion, Lagrangian and Eulerian Methods, Translation, Rotation and Rate of Deformation, Streamlines, Path lines and Streak lines.

**PROJECT 1:** A Report on Steady vs Unsteady Flow, Compressible vs incompressible Flow, Laminar vs Turbulent Flow, Newtonian vs Non-Newtonian Flow, Invisid vs Viscous Flow, Rotational vs Irrotational Flow. (Definition, Comparative Study & Examples)

# MODULE - II (5hr+0hr+0hr)

Fundamental equations of the flow of viscous compressible fluids: Equations of continuity, motion and energy in Cartesian coordinate systems, The equation of state, Fundamental equations of continuity, motion and energy in Cylindrical & Spherical coordinate systems.

#### MODULE - III (4hr+0hr+2hr)

2-D and 3-D inviscid incompressible flow: Basic equations and concepts of flow, Circulation theorems, Velocity potential, Rotational and Irrotational flows, Bernoulli's Equation.

**PROJECT 2:** A study on Stokes Circulation Theorem

# MODULE – IV (4hr+0hr+8hr)

Laminar Flow of Viscous Incompressible Fluids: Flow between parallel flat plates:Couette flow, Steady Flow in pipes: Hagen-Poiseuille flow, Unsteady motion of a flat Plate.

**PROJECT 3:** A study on plane Poiseuille flow.

**PROJECT 4:** A report on steady flow of viscous incompressible fluid between two porous parallel plates.

**PROJECT 5:** A study on laminar flow between two coaxial circular cylinders (i.e. an annulas).

**PROJECT 6:** A report on unsteady flow of a viscous incompressible fluid over an oscillating plate.

#### MODULE – V (5hr+0hr+0hr)

The Laminar boundary layer Flow: Properties of Navier-Stokes equations, Boundary layer equations in 2-D flow, Similarity of Flows, Reynold's Number, The boundary layer along a flat plate, Boundary layer on a surface with pressure gradient.

#### MODULE – VI (4hr+0hr+0hr)

Momentum Integral theorems for the boundary layer, Von karman-Pohlhausen method, Separation of boundary layer flow, Boundary layer control.

# MODULE - VII (4hr+0hr+0hr)

The origin of Turbulence, Reynold's modification of the Navier-Stokes equations for Turbulent flow, Reynold's stresses, Prandtl's mixing length theory.

#### **BOOK PRESCRIBED**

S. W. Yuan, "Foundations of Fluid Mechanics", Prentice – Hall of India Chapters: 3 (3.1 to 3.4), 5 (5.1 to 5.6), 7 (7.1 to 7.5), 8(8.1, 8.3, 8.4, 8.8),9 (9.1 to 9.6, 9.8, 9.9), 10(10.1 to 10.3(a))

#### **BOOK REFERENCE**

- 1. J. L. Bansal, "Viscus Fluid Dynamics", IBH Publication, Joypur.
- 2. M. D. Raisinghania, "Fluid Dynamics with Complete Hydrodynamics", S. Chand & Company Ltd, New Delhi.

Link: https://nptel.ac.in/courses/112/105/112105171/



# <u>Course outline</u>

# CUTM2381 GRID GENERATION AND CFD SIMULATION USING SIMULIA (0-2-2)

Subject Name	Code	Type of course	T-P-Pj (Credit)	Prerequisite
GRID GENERATION AND CFD SIMULATION USING SIMULIA	CUTM2381	Practice + Project	0-2-2	Nil

#### Objective

- To introduce the concepts of grid generation required for Computational Fluid Dynamics applications providing hands-on experience using Simulia.
- To produce a CFD simulation in order to generate an exact picture of a particular flow problem in various engineering fields.
- To apply for resolving different fluid flow related problems like flow velocity, density, temperature, and chemical concentrations for any area where flow is present.

#### **Course outcome**

After completion of the course, students will be able to

COs	Course outcomes
CO1	recognize the requirements of grid generation for Computational Fluid Dynamics
	applications.
CO2	explain the construction techniques of structured and unstructured grids using Simulia.
CO3	examine the control and efficiency of grid generation procedures.
CO4	execute CFD simulation in various industries in order to achieve flawless product
	designs using computational tools.
CO5	analyze flow simulations for different flow situations.

#### **Course Outcome to Program Outcome Mapping:**

COs	<b>PO1</b>	PO2	PO3	PO4	PO5	PO6	<b>PO7</b>	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	2	3	2	3	1	2	2			3		3	3	3	2
CO2			1		1	1				2	1	1	2	1	3
CO3	2	1	2	1		2	2			3		2	1	3	1
CO4	3	2	2		2					3	2	3	2	2	1
CO5	2	1		1	1	1	1			2		1	2	2	1

\*High-3, Medium-2, Low-1

# **Course Outline**

# Grid Generation & CFD Simulation using Simulia (0-2-2)

Practice: 2Hrs. Project: 4Hrs.

Practice 1: Getting Started with the 3D Experience Platform.Practice 2: CFD analysis of steady-state internal Laminar Pipe flow.Practice 3: Grid generation for pipe at Re=500.

**Project 1:** Analysis of pipe flow at Re= 500.

**Practice 4:** 3D Coarse/ Medium/ Fine unstructured mesh for Aerofoil. **Practice 5:** CFD analysis Steady-state external flow over an Airfoil.

**Project 2:** Estimation of Drag and lift coefficients in the flat plate at Re=10,000.

Practice 6: Grid Independence study for the above cases (pipe/airfoil) using different solver schemes.

**Practice 7:** Generation of 3D mapped meshing for Cylinder.

**Project 3:** Flow analysis over a circular cylinder at  $Re=10^7$ .

Practice 8: Grid generation for cross flow heat exchanger.

**Project 4:** Temperature analysis through cross-flow heat exchanger.

Practice 9: Generation of 3D Mesh for Ahmed Body.

**Project 5:** Turbulent analysis of Ahmed body.

Practice10. Grid generation for turbulent flow turbine blade

**Project 6:** Flow Analysis in the Turbine Blade.

**Practice 11:** Generation of 3D Sweep mesh for U-Bend Pipe. **Practice12:** Post processing results for above studies.



# **CUTM 2378 Research Methodology and IPR**

Subject Name	Code	Type of course	T-P-Pr (Credit)
<b>Research Methodology and IPR</b>	CUTM2378	Theory+Project	(2-0-2)

#### Objective

- To develop an appropriate framework for research studies
- To develop an understanding of various research designs and techniques.
- To identify various sources of information for literature review and data collection.
- To develop an understanding of the ethical dimensions of conducting applied research.
- To demonstrate enhanced Scientific writing skills
- warn the common mistakes in the field of research methodology.
- To make expertise in academic writing, patenting

#### Course outcome

COs	Course Outcomes
CO1	Search, select and critically analyse research articles and papers
CO2	Formulate and evaluate research questions
CO3	Develop the ability to apply the methods while working on a research project work
CO4	Describe the appropriate statistical methods required for a particular research design
CO5	Choose the appropriate research design and develop appropriate research hypothesis for a research project in research methodology
	for a research project in research methodology.

#### **Course Outcome to Program Outcome Mapping:**

COs	<b>PO1</b>	PO2	PO3	PO4	PO5	PO6	<b>PO7</b>	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	3	1		1	2	2			1	2		2	3	1
CO2	2			2	1	2	1				1	3	2	1	2
CO3	2	2	1	1		2						2	1	1	2
CO4							1					1	3	3	3
CO5		1		1		1	1			2		1	3	2	2

# \*High-3, Medium-2, Low-1

# **Course Outline**

# **CUTM 2378 Research Methodology and IPR**

#### Module 1: Elementary Research Methodology

Research Concept, Objective, characteristics, Steps and Significance of Research, Arbitrary and Scientific Research, Research approaches. Types of research: Historical, Descriptive, Analytical, Case Study, Quantitative vs. qualitative, Conceptual, Empirical Action Research, Research Methods vs Methodology. Research Problems: Selection and definition of the research problems, formulating a research problem, identifying variables and Constructing hypothesis; Choosing a mentor, lab and research question; maintaining a lab notebook; Selection of problems - stages in the execution of research.

#### Module II: Academic Writing and Presentation

Technical writing skills - types of reports; layout of a formal report; standard of Journal (Impact Factor, Citation Index), Scientific writing skills - importance of communicating science; problems while writing a scientific document; plagiarism, software for plagiarism; scientific publication writing: elements of a scientific paper including abstract, introduction, materials & methods, results, discussion, references; drafting titles and framing abstracts; publishing scientific papers - peer review process and problems, recent developments such as open access and non-blind review; characteristics of effective technical communication; scientific presentations; ethical issues; scientific misconduct.

#### Module III: Scientific communication skills

Concept of effective communication- setting clear goals for communication; determining outcomes and results; barriers to effective communication; non-verbal communication- importance of body language, power of effective listening; Presentation skills - formal presentation skills; preparing and presenting using over-head projector, PowerPoint; defending interrogation; scientific poster preparation & presentation; participating in group discussions; Computing skills for scientific research - web browsing for information search.

# Module IV: Introduction to IPR

Introduction to intellectual property; types of IP: patents, trademarks, copyright & related rights, industrial design, traditional knowledge, geographical indications. IP as a factor in R&D; IPs of relevance to biochemistry and few case studies; plant variety protection

#### **Module V: Types of Patents**

Basics of patents: types of patents; Indian Patent Act 1970; recent amendments; WIPO Treaties; Budapest Treaty; Patent Cooperation Treaty (PCT) and implications; filing of a patent application; role of a Country Patent Office; precautions before patenting-disclosure/non-disclosure - patent application- forms and guidelines including those of different regulatory bodies, fee structure, time frames; types of patent applications: provisional and complete specifications.

# PROJECTS

- 1. Write a review article and submit to a journal.
- 2. Write a book chapter/ book for publishing.
- 3. Write an original article for a journal.

#### **Books:**

- 1. Geoffrey Marczyk, David DeMatteo, David Festinger (2005) *Essentials of Research Design and Methodology*, John Wiley & Sons, Inc.
- 2. Carol Ellison (2010) McGraw-Hill's ConcisevGuide to WritingvResearch Papers, McGraw-Hill
- 3. Kothari CR (2016) Research Methodology: Methods and Techniques, New Age Pvt Ltd
- 4. Ganbawale RM, (2017) *Bioststistics and Research Methodology*, New Central Book Agency
- 5. Sinha, S.C. and Dhiman, A.K., (2002). *Research Methodology*, Ess Ess Publications. 2 volumes.
- 6. Trochim, W.M.K., (2005). *Research Methods: the concise knowledge base*, Atomic Dog Publishing. 270p.
- 7. Wadehra, B.L. (2000). *Law relating to patents, trademarks, copyright designs and geographical indications*. Universal Law Publishing.
- 8. Neuman, W.L. (2008). *Social research methods: Qualitative and quantitative approaches*, Pearson Education



**Course outline** 

# **CUTM1530 ADVANCED DIFFERENTIAL EQUATIONS**

Subject Name	Code	Type of course	T-P-Pj	Prerequisite
ADVANCED DIFFERENTIAL EQUATIONS	CUTM1530	Theory+Practice+ Project	2-1-1	Nil

# Objective

- To work with nonlinear ordinary differential equations.
- To develop and understand the qualitative behavior of the solution.
- To introduce wave equations, Laplace equations, Heat equations, Diffusion equations.

#### **Course outcome:**

After completion of the course, students will be able to

COs	Course outcomes
CO1	identify classes of non-linear ordinary differential equations.
CO2	select an appropriate method for the solution of non-linear ordinary differential
	equations.
CO3	classify non-linear partial differential equations of 2 <sup>nd</sup> order.
CO4	solve partial differential equations using method of separation of variables.
CO5	execute Python programming for solving ordinary and partial differential equations.

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	<b>PO7</b>	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	2		2			2				3			3	2	3
CO2	2	1		2	1	1				2	1	1	3	1	1
CO3	3	1	2	1		1	1			3		3	3	3	3
CO4	1	1	3		1					2		1	2	3	2
CO5	2	1		1						2		3	1	1	2

\*High-3, Medium-2, Low-1

# **Course outline**

#### Module I:

Introduction to Ordinary Differential Equations and Partial Differential Equations, First Order Nonlinear Ordinary differential equations such as Equations solvable for x, Equations solvable for y, Equations solvable for p. **Practice- 1:** Solve Ordinary Differential Equations in Python **Practice-2:** Solve Partial differential Equations by python

#### Module II

Partial differential equation of second order with variable coefficients- Monge's method and its properties.

Project 1: Monge's Method of Solution of Non-linear Partial Differential Equations of Order Two

#### **Module III**

Classification of linear partial differential equation of second order, Cauchy's problem, Method of separation of variables.

#### **Module IV**

Solution of one- dimensional Laplace equation by method of separation of variables and Fourier series

Project 2 : Solution of Laplace's Equation for a Disk

#### Module V

Solution of one- dimensional Wave equation by method of separation of variables and Fourier series

**Project 3:** D' Alembert's solution of the wave equation **Practice 3:** Solution of wave equation associated condition  $u(x,0)=\varphi(x),u_t(x,0)=\psi(x),u(0,t)=0,x\in(0,\infty),t>0$ **Practice 4:** Solution of wave equation associated condition  $u(x,0)=\varphi(x),u(0,t)=a,x\in(0,\infty),t\geq0$ 

#### Module VI

Solution of one- dimensional Diffusion equation by method of separation of variables and Fourier series

**Project 4:** Solution of Diffusion equation in n-dimensional **Practice 5:** Solution of one-dimensional diffusion equation by using boundary conditions  $u(x,0)=\varphi(x),u(0,t)=a,x\in(0,\infty),t\geq 0$ **Practice 6:** Solution of one-dimensional diffusion equation  $u(x,0)=\varphi(x),u(0,t)=a,u(1,t)=b,0<x0$ 

# **Module VII**

Solution of one- dimensional Heat equation by method of separation of variables and Fourier series

**Project 5:** Two dimensional Heat equations- Polar form **Project 6:** Temperature distribution in Rectangular plate

# **Text Books**

- *1.* Differential Equations and Their Applications, by Martin Braun, Springer, 4e, ISBN 9781111827052 (1993).
- 2. S. L. Ross: Differential Equations, Blaisdell Publishing Company, Londan, 1964.

#### **Reference books:**

- S.J. Farlow: An Introduction to Ordinary Differential Equations, PHI
   M.D. Raisinghania: Ordinary and Partial Differential Equations, S. Chand & Co.
   V. Sundarapandian: Ordinary and Partial Differential Equations, McGraw-Hill



# **CUTM1531 GRAPH THEORY**

Subject Name	Code	Type of course	T-P-Pj (Credit)	Prerequisite
GRAPH THEORY	CUTM1531	Theory & Practice	3-1-0	Nil

# **Objective:**

- To understand the concept of graphs, their properties and their applications as models of networks.
- To define the basic concepts of graphs, directed graphs, and weighted graphs, the properties of bipartite graphs, particularly in trees.
- To apply the technique of generating functions and graph theory-based tools in solving practical problems.

#### **Course outcome:**

After completion of the course, students will be able to:

COs	Course outcomes
CO1	explain basic definitions and concepts of graph theory and Write in a coherent and
	technically accurate manner.
CO2	describe how to develop graph theoretical algorithm and discuss about many
	different coloring problems for graphs.
CO3	demonstrate that many problems-theoretical or real-life, can be analyzed and
	solved by using graphs.
CO4	develop the skill of translating problems to graph-theoretic problems and
	translating the solutions to the real-life problems.
CO5	use abstract concepts of graph theory in modeling and solving non-trivial problems
	in different field of study

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3		1			2				1		2	2	2	3
CO2	3		3	1	1	1	3			2	1	1	3	1	1
CO3	2	1		1			1			1		3	2	2	3
<b>CO4</b>	2		1			2					1	2	1	3	2
CO5	3				1		1			2		1	3	2	3

# Module-I

Introduction to Graphs and Definition of graphs;Basic terminologies and types of graphs;Degree of a vertex,Isolated and Pendent vertices;Sub graphs and graph Isomorphism.

**Practice 1:** Determine if two graphs are isomorphic and identify the isomorphism

# Module-II

Directed Graphs and Types of Digraphs;Out-degree, In-degree, Connectivity and Orientation;Digraphs and Binary relations, Directed paths and contentedness;Euler Digraphs, De-Brujin sequences;Tournaments.

Practice 2: Ways to Represent Graphs using Python

#### Module-III

Basic concepts of Planar Graphs; Kuratowski's Two graphs ;Representation of Planar Graphs; Detection of planarity ;Euler's formula for planar graphs;

Practice 3: A look in to Planar Graphs and Euler's Relationship

# Module-IV

Distance, cut-vertices, cut-edges, blocks; weighted graphs, connectivity; Dijkstra's shortest path algorithm; Floyd-War shall Shortest path algorithm;

# Module-V

Proper Coloring of graphs;Chromatic numbers of a graph;Chromatic polynomial;Chromatic Partitioning;Four Colour theorem.

Practice 4: Finding Chromatic number using python-networks.

# **Module-VI**

Definition and properties of trees; Rooted and Binary trees; Counting trees, Spanning trees;

**Practice 5:** Applications of graphs with Euler and Hamiltonian path and circuits (Chinese postman Problem)

# Module-VII

Minimum spanning trees;Fundamental Circuit;Cut set and Separability;

Practice 6: Application of Minimum spanning tree in a Net work model

# Text Book:

 Deo, N., "Graph Theory with Applications to Engineering and Computer Science", Prentice Hall India 2004 Chapters: 1(1.1,1.2,1.3,1.4,1.5) ,2 (2.1,2.2,2.4,2.4,2.6,2.9), 3 (3.1,3.2,3.5,3.7,3.8,3.9,3.10), 4 (4.1,4.4,4.5), 5(5.2,5.3,5.4,5.5), 7(7.1,7.2), 8 (8.1,8.2,8.3,8.6), 9 (9.1,9.2,9.3,9.4, 9.5)

#### **Reference Books**:

- 2. West, D. B., "Introduction to Graph Theory ", Prentice Hall India (2nd Edition 2009)
- 3. Aldous, J. M., Wilson, R. J. and Best S., "Graphs and Applications: An Introductory Approach", Springer2003.
- 4. Deistel, R., "Graph Theory", Springer (4th Edition) 2010.
- 5. Chartrand, G. and Zhang, P., "Introduction to Graph Theory", Tata McGraw Hill2007.
- 6. Bondy, J. A. and Murty, U. S. R., "Graph Theory", Springer 2011



# **CUTM1532 OPTIMIZATION TECHNIQUES**

Subject Name	Code	Type of Course	T-P-Pj (Credit)	Prerequisite
OPTIMIZATION TECHNIQUES	CUTM1532	<b>T</b> + <b>P</b>	3-1-0	Nil

# **Course Objective**

- To introduce a brief understanding about Non Linear Programming Problems.
- To cater the characteristics of Non Linear Programming Problems and its Applications.
- To apply the evolutionary optimization techniques in machine learning prediction model

#### **Course outcome:**

After completion of the course, students will be able to

Cos	Course outcomes
CO1	explain the necessary and sufficient optimality conditions for Nonlinear
	programming.
CO2	use gradient method in solving applied engineering and fluid dynamic problems.
CO3	apply the optimization techniques learnt in this course to formulate new applications
	as optimal decision problems and seek appropriate solution algorithms.
CO4	examine evolutionary optimization techniques to optimize the forecasting models in
	machine learning.
CO5	develop game theory model to make decision in critical business problems

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	2	1			2				2		3	3	3	3
CO2	2			2	1						1	1	2	1	3
CO3	1	1		1		2	1			1			2	3	2
<b>CO4</b>			1									2	1	3	3
CO5		1			1							1	3	2	3

# Course Outline CUTM1532 Optimization Techniques (3-1-0)

#### Module-I (5 Hours)

Non Linear Constrained Optimization Problem: Constrained optimization using Lagrange Method, Lagrange Multiplier Equality Constraints, Constrained optimization using Kuhn Tucker Method, Kuhn Tucker inequality Constraints.

#### Practice-1: (2 Hours)

Solving minimization constrained optimization problem using python

#### Practice-2: (2 Hours)

Solving maximization constrained optimization problem using python **Module-II (5 Hours)** 

Direct Search Method for Unconstrained Optimization Problem: Univariate Search Method, Golden Section Search Method and Application of Golden Section Search Method.

# Practice-3: (2 Hours)

Solving nonlinear system of equations using Python

#### **Module-III (4 Hours)**

Gradient Method for Unconstrained Optimization Problem: Gradient Descent Method, Algorithm for Gradient Descent Method, Steepest Descent Gradient Method.

#### Practice-4: (2 Hours)

Implementing Gradient Descent algorithm in Python

#### **Practice-5**: (2 Hours)

Linear Regression using Gradient Descent in Python

#### Module-IV (4 Hours)

Sequencing Models: Problems with n' Jobs through Two Machines, Problems with 'n' Jobs through Three Machines, Problems with Two Jobs through 'm' Machines.

#### **Module-V (4 Hours)**

Particle Swarm Optimization: Particle Swarm Optimization Theory, Particle Swarm Optimization Algorithm, Application of Particle Swarm Optimization,

**Practice-6 & 7**: (2+2 Hours) Implementing the Particle Swarm Optimization (PSO) Algorithm in Python

#### Module-VI (4 Hours)

Game with Pure Strategy: Game and Strategy, Maximin-Minimax principle, Two person zero-sum game with Saddle Point, Solving matching coin problem using game theory.

#### **Module-VII (4 Hours)**

Game with Mixed Strategy: Mixed Strategy Game, Game without Saddle Point, Graphical Method to Solve Mixed Strategy Game, Dominance Principle to Solve Mixed Strategy Game.

# **Text Books:**

- 1. Kanti Swarup, P.K. Gupta and Man Mohan-Operations Research, S. Chand and Co. Pvt.Ltd.
- 2. Engineering Optimization Theory and Practice by Singiresu S. Rao, JOHN WILEY & SONS, INC., Fourth Edition

# **Reference Book**:

1. Mathematical Programming by N. S. Kambo, East West Press.



# CUTM1533 ADVANCED STATISTICAL METHODS

Code	Course Title	T-P-Pj (Credit)	Prerequisite
CUTM1533	ADVANCED STATISTICAL METHODS	2-1-1	NIL

# Objective

- To develop the ability for numerical and visual data presentation.
- To determine the situations in which the various statistical techniques will be applied.
- To enhance the ability critically about data-based claims and quantitative arguments.

#### **Course outcome**

After completion of the course, students will be able to

COs	Course outcomes
CO1	describe the statistical methods and hypothesis testing to business problems
	use Chi Squared Tests and to understand different type of data.
CO2	interpret the complexities of Analysis of Variance (ANOVA)
CO3	compare different types of regression analysis
CO4	
	extract the complexities of multiple regression (MR).

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	2	1			2		3				3	2	1	1
CO2	2	1		2	1	2		2			1	1	2	1	3
CO3	2	1	2	1		1	1	2					1	2	3
<b>CO4</b>	3	1	2		2			3				3	2	2	1
CO5		1		1			2	2				2	3	1	1

\*High-3, Medium-2, Low-1

# **Course Content**

# Module I: (2 hrs+0 hrs+2hr)

Statistics: Population, Sample, Sampling, Estimators and Estimates, Maximum Likelihood, Confidence Intervals

**Project-1** Application of Confidence intervals as a tool in decision making

# Module II: (3 hrs+0hr+2hr)

Hypothesis Testing: Null and the alternative hypothesis, Rejection region and significance level, Chi-Square Test

# **Project-2**

Hypothesis Testing in Quality Management

**Module III: (4 hrs+4 hrs+0hr)** Regression: Multiple Regression and Logistic Regression

**Practice-1** Multiple Regression Analysis in Python

**Practice-2** Logistic Regression using Python

**Module IV: (3 hrs+4 hrs+2hr)** Analysis of Variance (ANOVA): F- Distribution, One way ANOVA, Two Way ANOVA

**Practice-3** One way ANOVA using Python

**Practice-4** Two way ANOVA using Python

**Project-3** The utility of multivariate statistical techniques in hydro geochemical studies

**Module V: (3 hrs+2 hrs+2hr)** Covariance: (ANCOVA): Analysis of Covariance (ANCOVA), Bivariate Pearson Correlation, Alternative Correlation Coefficients

**Practice-5** Python Analysis of covariance (ANCOVA)

**Project-4** Application of Analysis of covariance (ANCOVA) in psychological research

**Module VI: (3 hrs+0hr+2hr)** Multivariate analysis of variance (MANOVA): One-way MANOVA, Two-way MANOVA

**Project-5** Comparison of MANOVA to ANOVA Using an Example

# Module VII: (3 hrs+2 hrs+2hr)

Time Series Analysis: Introducing Time Series Analysis, Components of Time Series Analysis,

Multivariate Time Series Analysis

# **Practice-6**

Time Series Analysis using Python

# **Project-6**

A Report on Applications of Time Series Analysis in Census Analysis

# **Text Books:**

- 1. Statistical Methods By S.P. Gupta (31st Edition) ; Publisher: Sultan Chand & Sons
- 2. Mathematical Statistics by S.C. Gupta & V.K. Kapur (10th Edition); Publisher: Sultan Chand & Sons.

# **Reference Books:**

1. Understanding And Using Advanced Statistics by Jeremy Foster Emma Barkus Christian Yavorsky, SAGE Publications



# **CUTM1534 APPLIED NUMBER THEORY**

Subject Name	Code	Type of course	T-P-Pj (Credit)	Prerequisite
APPLIED NUMBER THEORY	CUTM1534	Theory+Practice	3-1-0	Nil

# Objective

- To analyze, evaluate, or solve problems with in given a set of circumstances or data.
- To understand and utilize mathematical functions and empirical principles and processes.
- To Enhance and reinforce the student's understanding of concepts through the use of technology when appropriate

#### **Course outcome:**

After completion of the course, students will be able to

	$\mathbf{I}$ , $\mathbf{i}$
COs	Course outcomes
CO1	describe the properties of prime number
CO2	implement Euclidian algorithm
CO3	solve Systems of linear Congruence's
CO4	distinguish Pseudo prime from prime numbers
CO5	appraise different types of cipherings.

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	1	1			2				1		2	2	3	2
CO2	2	2		2	1	2					1	3	2	1	1
CO3	2	1	2	1		1	1			1			2	3	3
CO4		2			3						1	1	3	1	2
CO5	2		2		1		3				2	3	1	2	3

# CUTM 1534 APPLIED NUMBER THEORY (3-1-0)

#### MODULE – I (4hr+2hr+0hr)

Divisibility, Representations of Integers, Computer Operations with Integers, Prime Numbers

Practice-1: Write a program to decide whether an integer is prime using trial division of the integer by all primes not exceeding its square root.

#### MODULE – II (6hr+4hr+0hr)

Greatest common divisor, Euclidean Algorithm, Modified Euclidean Algorithm, Prime factorization, Factorization of Integers

Practice-2: Write a program to find the greatest common divisor of two integers using the Euclidean algorithm. Practice-3: Find the prime factorization of a positive integer. MODULE – III (5hr+2hr+0hr)

Congruence's, Properties of Congruence's,System linear Congruence's Chinese Remainder Theorem. Practice -4: Write a program to solves systems of linear congruence

# MODULE - IV (5hr+0hr+0hr)

Wilson's Theorem, Fermat's Little Theorem, Pseudo prime, Carmichael number

# MODULE - V (4hr+2hr+0hr)

Euler's Theorem, Euler Phi-function, Perfect Numbers, Mersenne Primes Practice -5: Write programs to find values of the Euler phi-function

#### MODULE - VI (3hr+2hr+0hr)

Character Ciphers, Block Ciphers, Exponentiation ciphers, Public-Key Cryptography (RSA Cryptosystem).

Practice-6: Write a program for RSA crypto system/Algorithm

# MODULE - VII (3hr+0hr+0hr)

Knapsack ciphers, Some applications to computer science.

# **BOOK PRESCRIBED**

 Elementary Number Theory and Its Applications by Kenneth H. Rosen, ADDISON-WESLEY PUBLISHING COMPANY ISBN 0-201-06561c chapter- 1(1.2-1.5), 2(2.1-2.4), 3,5,6(6.1-6.3),7

#### **BOOKS FOR REFERENCE**

- 1. Elementary Number Theory by David M. Burton, fifth edition, McGraw-Hill Publication, ISBN- 0-07-232569-0
- 2. A Course in Number Theoretic Cryptography by Neal Koblitz, Springer Verlag, GTM



# **CUTM1535 ADVANCED COMPLEX ANALYSIS**

Subject Name	Code	Type of course	T-P-Pj (Credit)	Prerequisite
ADVANCED COMPLEX ANALYSIS	CUTM1535	Theory+Project	3-0-1	Nil

#### Objective

- To introduce the concept of residue.
- To know about special functions like Riemann zeta function
- To provide brief idea about Laurent series

#### **Course outcome**

After completion of the course, students will be able to:

COs	Course outcomes
CO1	explain basic concept of residue.
CO2	classify different types of real integrals.
CO3	demonstrate Mean-Value Property and Poisson's formula
CO4	use Taylor and Laurent series for expressing analytic functions
CO5	examine the convergence of Riemann Zeta function.

# **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	<b>PO7</b>	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1			3			2	1			1		2	3	2	3
CO2		2		2	1					2	1	1	3	1	1
CO3	2	2	1	1	1	1	2			1			2	3	2
CO4	2		1								1	3	2	2	2
CO5	2	1		1	2	1	1			1		2	2	3	3

\*High-3, Medium-2, Low-1

# CUTM1535 Advanced Complex Analysis (3-0-1)

#### MODULE - I (3hr+0hr+0hr)

Index of a point with respect to a closed curve, Simply connected region, General statement of Cauchy's theorem.

#### MODULE - II (4hr+0hr+2hr)

Residue, process for finding out the residues, Residue theorem, the Argument Principle. **PROJECT 1:** Study on Residues and their applications.

# MODULE - III (5hr+0hr+2hr)

Definite Integrals: Evaluation of definite integrals (Types -1, 2, 3, 4, 5). **PROJECT 2:** Evaluation of different types of real definite integrals using Residue theorem.

#### MODULE - IV (4hr+0hr+2hr)

Harmonic functions, conjugate differential, The Mean-Value Property, Poisson's formula. **PROJECT 3:** A study on Harmonic functions.

#### MODULE – V (6hr+0hr+2hr)

Taylor Series, Taylor's theorem, Laurent series, Laurent's theorem, infinite products, theorems on infinite products.

**PROJECT 4:** A study on Laurent series expansion of different types of meromerphic functions.

#### MODULE - VI (3hr+0hr+2hr)

Entire functions: Jensen's formula, Riemann Zeta function, theorem on Riemann Zeta function. **PROJECT 5:** A study on Riemann Zeta function and it's properties.

# MODULE – VII (6hr+0hr+2hr)

Simply periodic function, Module, Discrete module, Unimodular transformation, Canonical basis, theorem on Canonical basis.

**PROJECT 6:** A study on discrete modules.

#### **BOOK PRESCRIBED**

 1 L. V. Ahlfors, "Complex Analysis", McGraw-Hill, Inc. Chapters: 4 (2.1, 4.2 to 4.5, 5.1 to 5.3, 6.1 to 6.3), 5 (1.2, 1.3, 2.2, 3.1, 4.1), 7 (1.1, 2.1, 2.2, 2.3)



# CUTM1536 TOPOLOGY

Subject Name	Code	Type of course	T-P-P	Prerequisite
TOPOLOGY	CUTM1536	Theory + Project	3-0-1	NIL

# Objective

• To introduce elementary properties of topological spaces and structures

• To introduce the student to maps between topological spaces

• To develop the student's ability to handle abstract ideas of Mathematics and Mathematical proofs

#### **Course outcome:**

After completion of the course, students will be able to

Cos	Course outcomes
CO1	describe elementary properties of topological spaces and structures
CO2	solve the problems on Countable compact spaces, continuous functions and
02	Homeomorphisoms
CO3	compare To and T <sub>1</sub> - spaces and sequence
CO4	implement Urysohn's metrization theorem, Urysohn's Lemma, Metrization, Tietze
C04	extension theorem
CO5	execute proves on Metric topology, Metric products, Dense set

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3		3		1	1	1	1				3	3	3	2
CO2	2	2		2			2				1	1	3	1	1
CO3	2		1		3	1	2						2	2	3
CO4		3	1								1	2	2	2	3
CO5	2	1		1	2		1					3	2	3	2

\*High-3, Medium-2, Low-1

# Module I

Introduction of topological space, Open sets and limit points, Closed sets and closure, Bases and relative topologies

**Project 1:** Applications of Topology to the Analysis of 1-Dimensional Objects

Project 2: Topologies sequentially equivalent to Kuratowski Painlev´e convergence

# Module II

Connected sets and components, compact and Countable compact spaces, continuous functions, Homeomorphisoms

**Project 3: Sober topological space** 

# Module III

To-and T1-spaces and sequence, Separation axioms

Module IV

Axioms of count ability, Regular and normal spaces, Completely regular spaces **Project 4: Upper Topology** 

# Module V

Urysohn's metrization theorem , Urysohn's Lemma, Metrization, Tietze extension theorem Project 5: Scott topology Project 6: Scott continuity

# Module VI

Finite products, product invariant properties, product topology

# Module VII

Metric topology, Metric products, Dense set

# Text Books

- 1. W.J. Pervin, Foundations of General Topology, Academic Press. Chapters: 3 (3.1, 3.2 and 3.4), 4(4.1 to 4.4), 5 (5.1 to 5.3, 5.5 and 5.6), 8 (8.1 to 8.4), 10 (10.1 only).
- 2. J. R. Munkres; Topology A First Course, Prentice Hall of India, 1996.

# **Reference Book**

- 1. K. D. Joshi, Introduction to General Topology, Wiley Eastern Ltd., 1983.
- 2. <u>http://mat.uab.cat/ret/sites/default/files/material/otras\_contribuciones/ProceedingsWI\_AT10.pdf</u>



# **CUTM1537 DIFFERENTIAL GEOMETRY**

Subject Name	Code	Type of course	T-P-Pj	Prerequisite
DIFFERENTIAL	CUTM 1537		3-0-1	NIL
GEOMETRY		Theory + Project		

# Objective

- To introduce the basic ideas and techniques of Differential Geometry for use in many other courses.
- To study about different geometrical skills for figure and their representation in mathematical equations
- To study about notations and operations of Tensor.

#### **Course outcome:**

After completion of the course, students will be able to

COs	Course outcomes
CO1	describe equation of normal, binormal and tangent to a curve.
CO2	explain Curvatures and Torsion of curves.
CO3	sketch the shape of geometrical figure from equation.
CO4	differentiate curves of different in nature.
CO5	to distinguish different type of tensor.

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1			3		1	1	1			3		3	3	3	2
CO2		2		2			2			3	1	1	3	1	1
CO3	2		2		1	1	1			3	2	2	2	3	3
CO4	2	3	1			2				3	1	2	2	1	3
CO5	3	2	2	3		2				3	3	2	3	3	3

# **Module-I**

Introduction to Differential Geometry,Osculating plane and Rectifying Plane **Project 1**:.finding the direction of tangent , normal and binormal at any point of curve

# Module-II

Curvatures of a curve at a point, Torsion of a curve at a point, Expression of Curvature and Torsion in terms of arc length parameter, Expression of Curvature and Torsion in terms of arbitrary parameter

**Project 2**: Compute the Curvature of an ellipse.

# Module-III

Spherical Indicatrix, Evolutes , Involutes **Project 3**: Determine the evolutes of the given curve.

# Module-IV

Betrand Curve, Osculating Spheres, Osculating circles. **Project-4**: Show that the tangent to the locus of osculating sphere passes through the centre of the Oscilating Circle.

# Module-V

Surface: Tangent planes and Normals, The two fundamental forms **Project 5**: Find the normal to a given surface

# **Module-VI**

Tensor : Definitions and explanations, Vector Space, Free systems, Basis and Dimension, Suffix Conventions, Transformation law for change of Basis Vectors and Components, Dual Spaces

# **Module-VII**

Transformation law for change of Basis in dual Space, Isomorphism, Tensor Product of Vector Spaces, Real Valued Bilinear Functions, Special Tensors

Project-6: Show that the velocity of a fluid at any point is component of a contravariant vector

# **BOOK PRESCRIBED**

- 1. A text book of vector calculus-Shanti Narayana and J.N.Kapoor Chapters: II and III
- 2. An Introduction to Differential Geometry by T.G. Willmore-Oxford University Press (1983) Chapters: V

# **BOOK FOR REFERENCE**

- 1. Differential Geometry-P.P.Gupta,G.S.Malik, S.K.Pundir
- 2. Tensor Analysis- Edward Nelson( Princeton University Press & University of Tokyo Press),1967
- 3. Introduction to Tensor Analysis and the Calculus of Moving Surfaces-<u>Pavel Grinfeld</u>, Springer



# CUTM1538 ADVANCED ALGEBRA

Subject Name	Code	Type of course	T-P- P(Credit)	Prerequisite
ADVANCED ALGEBRA	CUTM1538	Theory+Project	3-0-1	Nil

# Objective

- To introduce students to the language and precision of modern algebra. This means that the course will be proof-based, in the sense that students will be expected to understand, construct, and write proofs.
- To balance the understanding with the communication of mathematical statement is true or false.
- To know how to construct a legitimate proof involves different skills and expertise than the discovery part of the process.

#### **Course outcome:**

After completion of the course, students will be able to

COs	Course outcomes
CO1	explain about Ring and some special classes of Ring.
CO2	locate and use theorems to solve problems in number theory and theory of
	polynomials over a field.
CO3	implement Sylow's Theorems
CO4	use field of Quotients and Integral Domain in Ring
CO5	compare linear dependent and independent vectors

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	2	1			2		1		1		1	3	3	2
CO2	2			2	1	2	2				1	1	2	1	3
CO3	3	3	2		2			2				2	2	3	2
CO4	2		2			1					2	2	2	3	3
CO5	1	1		2	2	1	1			1		3	1	2	3

# CUTM1538 Advanced Algebra (3-0-1)

# MODULE – I (6hr+0hr+2hr)

Group Theory: Another Counting Principle, Sylow's Theorems. **Project 1** : A Notes on the Proof of the Sylow Theorem

# MODULE – II (6hr+0hr+2hr)

Ring Theory: Introduction to Ring, Some special classes of ring, Ring homomorphisms. **Project 2**: A study on ring theory and it's property

# MODULE – III (3hr+0hr+2hr)

More Ideals and Quotient Rings, The Field of Quotients of an Integral Domain. **Project 3:** The Quotient Field of an Intersection of Integral Domains

# MODULE - IV (4hr+0hr+2hr)

Euclidean Rings, A Particular Euclidean Ring, Polynomial Rings. **Project 4**: On the Existence of a Euclidean Algorithm in Number Rings with Infinitely Many Units

# MODULE – V (4hr+0hr+0hr)

Polynomial Rings over the Rational Field, Polynomial Rings over Commutative Rings.

# MODULE - VI (3hr+0hr+2hr)

Fields: Extension Fields, Roots of polynomials **Project 5:** A study on Structure of a Finite Field

# MODULE – VII (4hr+0hr+2hr)

Vector Spaces: Elementary Basic Concepts of Vector Space, Linear Independence and Basis, Dual Spaces, Inner Product Spaces **Project 6**: Notes on dual spaces

# **BOOK PRESCRIBED**

1. Topics in Algebra – I. N. Herstein (John Wiley and Sons or Vikas Publication), 2<sup>nd</sup> Edition Chapters: 2 (2.11 to 2.12), 3 (3.1 to 3.11), 4 (4.1 to 4.4), 5(5.1 and 5.3)

# **BOOKS FOR REFERENCE**

- 1. S.Singh and Q. Zameeruddin, Modern Algebra, Vikas Publishing House, 1990
- 2. P.B. Bhattacharya, S. K. Jain and S. R. Nagpal, Basic Abstract Algebra, Cambridge University Press, 1995.

# (Domain Courses) NET Domain

Sl.No	Code	Subject Name	Cerdit	Course Type (Th+Pr+Pj)
1	CUNT2480	Functional Analysis	4	3-0-1
2	CUNT2481	Integral Equation	4	3-0-1
3	CUNT2482	Advanced Calculus	4	3-0-1
4	CUNT2483	Operation Research	4	3-0-1
5	CUNT2484	Descriptive statistics & Data analysis	4	3-0-1
		Total	20	



# **CUNT2480 Functional Analysis**

Subject Name	Code	Type of course	T-P-Pj (Credit)	Prerequisite
FUNCTIONAL ANALYSIS	CUNT2480	Theory+Project	3-0-1	Nil

# Objective

- To introduce different analytical structures, concepts and Theorems.
- To enable students to solve problems involving linearly independent and dependent sets and basis.
- To emphasis not only on finding explicit solutions to specific problems, but also on determining which problems can be solved and what general properties solutions may share.

#### **Course Outcome**

After completion of the course, students will be able to

COs	Course outcomes
CO1	describe fundamental concepts like linear space, linear map, and Continuous map.
CO2	explain the terms like dimension, basis, compactness, normed space.
CO3	solve problems involving linearly independent and dependent sets, basis.
CO4	examine bounded linear maps, Lp spaces.
CO5	compare Sequence spaces, Lp space, Function spaces and Inner product spaces.

# **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	2	1	3		2			2	3	2	3	2	3	2
CO2	3	2	1	3		2			2	3	2	2	2	3	2
CO3	3	3	2	2	2	1			2	2	3	2	3	2	1
CO4	3	3	2	2	2	1			2	3	2	3	2	3	2
CO5	3	2	1	3		2			2	3	2	2	2	2	2

# \*High-3, Medium-2, Low-1

# Course outline CUNT2480 Functional Analysis

#### **MODULE-I**

Linear space, Hamel basis, Span of a linear space, Quotient space, Product space. **Project-1**: A study on Linear spaces.

#### **MODULE -II**

Linear map, Range space, Zero space, Hyperspace, Linear maps on finite dimensional linear spaces. **Project-2:** A study on Linear maps. **MODULE – III** Compactness, Some fundamental theorems regarding compactness. **Project-3:** A study on Compactness.

#### MODULE-IV

Normed space, Euclidian norm, Sequence spaces, Lp space, Function spaces, Inner product spaces. **Project-4**: A study on Normed spaces.

#### MODULE – V

Quotient norm, Riesz Lemma, Some theorems regarding normed spaces.

#### **MODULE – VI**

Continuity of linear maps, Complete space, Some fundamental theorems. **Project-5:** A study on Continuous linear maps.

#### **MODULE – VII**

Bounded Linear maps, Some fundamental theorems, **Project-6**: A study on Bounded Linear maps.

#### **BOOK PRESCRIBED**

 Functional Analysis—B. V. Limayee (New Age— International Limited, Publishers, Second Edition) Chapters: 2, 2.1, 2.2, 2.3, 2.4, 2.5, 3.5, 3.6, 3.7, 5, 5.1, 5.2, 5.3, 5.4, 6, 6.1, 6.2, 6.3, 6.6, 6.7, 6.8.



# **CUNT2481 INTEGRAL EQUATION**

Subject Name	Code	Type of course	T-P-Pj (Credit)	Prerequisite
INTEGRAL EQUATION	CUNT2481	Theory + Project	3-0-1	Nil

# Objective

- To identify different type of Integral equations.
- To solve different type of Boundary value problems of Integral Equations in nature.
- To convert differential equations into Integral equations.

# **Course Outcome**

After completion of the course, students will be able to

COs	Course outcomes
CO1	Classify the integral equations.
CO2	Explain conversion of multiple integrals into single ordinary integral
CO3	Solve Integral equations of different types
CO4	Differentiate the solution of homogeneous and non-homogeneous Integral Equations
CO5	Evaluate Volterra Integral Equation of the Second Kind

Course	Outcome	to Program	Outcome	Manning:
Course	Outcome	to i rogram	Outcome	mapping.

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	2	2	1	3	3	1					2	3	1	1
CO2	2	2	1	2	3						1	1	2	1	2
CO3	3	2	1	2	1	1	2					3	2	1	2
<b>CO4</b>	2	1	1	1	1	1						2	3	1	2
CO5	2	1		1	2	1	1					1	3	1	2

\*High-3, Medium-2, Low-1

#### **Course outline**

# **INTEGRAL EQUATION**

# MODULE-I

Introduction, Definitions of Integral Equation, Linear, Non Linear Equations, Fredholm Integral Equation, Volterra Integral Equation, Singular Integral Equation, Special Kinds of Kernels, Integral equations of Convolution type, Iterated Kernel sand Resolvent Kernel. **Project 1**: Prepare a detail report of different kind of Integral Equations.

#### **MODULE-II**

Eigen values, Leibnitz's rule of differentiation under integral sign, Formula for converting multiple integrals into single ordinary integral, Regularity conditions, Inner product of two functions, Definition and some simple examples of Solution of Integral Equations.

**Project 2**: Prepare a report on Leibnitz's rule of differentiation under integral sign and Formula for converting multiple integral into single ordinary integral.

#### **MODULE-III**

Conversion of Ordinary differential equations into integral equations.

**Project 3**: Prepare a report on advantages of Conversion of Ordinary differential equations into integral equations

#### **MODULE-IV**

Homogeneous Fredholm Integral Equations of the Second kind with Separable Kernels. **Project-4**: Prepare a report on advantages of Fredholm Integral Equations of the Second kind.

#### **MODULE-V**

Fredholm Integral Equations of the Second kind with Separable Kernels.

#### **MODULE-VI**

Method of Successive approximations: Concepts, Solution of Fredholm Integral Equation of the Second Kind by Successive Substitutions.

**Project 5:** Prepare a report on Solution of Fredholm Integral Equation of the Second Kind by Successive Substitutions.

#### **MODULE-VII**

Solution of Volterra Integral Equation of the Second Kind by Successive Substitutions.

**Project-6**: Prepare a report on Solution of Volterra Integral Equation of the Second Kind by Successive Substitutions

#### **BOOK PRESCRIBED**

1. Integral Equations and Boundary Value Problems by M.D. Raisinghania, S.Chand & Company pvt Ltd. Ch-1, Ch-2, Ch-3, Ch-4 Ch-5 (5.1-5.7)

#### **BOOK FOR REFERENCE**

- 1. Introduction to Integral Equations with Applications , A.J. Jerri, Wiley-Interscience Publication, 1999
- 2. Linear Integral Equations, W.V Lovitt, McGraw Hill, New York



# **CUNT2482 ADVANCED CALCULUS**

Subject Name	Code	Type of course	T-P-Pj (Credit)	Prerequisite
ADVANCED CALCULUS	CUNT2482	Theory+ Project	3-0-1	Nil

# Objective

- To study about Taylor's theorem. It provides a framework for application of Taylor's theorem in problems
- To construct an over view on Green, Gauss & Stokes Theorem
- To familiarize on Differentiation of Transformations

# **Course Outcome**

After completion of the course, students will be able to

COs	Course outcomes
CO1	describe derivatives of functions on R <sup>n</sup> , Differentiation of composite functions,
	Taylor'stheorem.
CO2	solve problems related to theorems on Green, Gauss & Stokes.
CO3	discuss problems on differentiation of transformations, Linear functions and
	transformations.
CO4	implement the major problems on Power Series, Improper integrals with parameters.
CO5	experiment other important classes of functions such as Gamma Function. Beta
	Function

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	2	3		3	3	1					2	2	3	1
CO2	2	2		2	3						1	1	1	1	2
CO3	2	2	1		1	1	2					3	2	3	2
CO4	2		1	1		3						2	3	1	2
CO5	2	1		1	2	1	1					1	3	3	2

**Course Outcome to Program Outcome Mapping:** 

#### \*High-3, Medium-2, Low-1

# Course outline

# **ADVANCED CALCULUS**

# **MODULE-I**

Derivatives of functions on R<sup>n</sup>, Differentiation of composite functions, Taylor's theorem, Differential forms.

#### PROJECT

A brief report on Taylor's Theorem.

# **MODULE-II**

Theorems of Green, Gauss & Stokes, **PROJECT** An over view on Green, Gauss & Stokes Theorem.

# **MODULE-III**

Differentiation of Transformations, Linear functions and Transformations, Differential and Transformations.

MODULE– IV Inverse of Transformations, Implicit function Theorems, Functional Dependence. PROJECT A project report on Implicit function Theorem.

MODULE– V Set functions, Transformations and Multiple integrals, curves and Arc Length. PROJECT A discussion on curves and Arc length

MODULE– VI Surfaces and surface area, integrals over curves and surfaces. PROJECT A note on integrals over curves.

MODULE– VII Power Series, Improper integrals with parameters, The Gamma Function. PROJECT A brief report on Gamma function.

# **BOOK PRESCRIBED**

1. Advanced calculus – R. C. Buck (Mc. Graw hill– Kogakusha Ltd.)Chapters:3 (3.3, 3.4, 3.5), 6 (6.3,6.4),7,8, 9 (9.2, 9.4, 9.5)



# **CUNT2483 OPERATION RESEARCH**

Subject Name	Code	Type of course	T-P-P (Credit)	Prerequisite
OPERATION RESEARCH	CUNT2483	Theory + Project	3-0-1	Nil

# **Objective:**

- To demonstrate the utilization of Linear Programming Problems in industry and business.
- To apply the inventory control techniques in real-life application problems.
- To apply queuing model to find the optimum service rate and to minimize the number of servers.

# **Course outcome**

After completion of the course, students will be able to

Cos	Course outcomes
CO1	explain the concept of extreme values of some real-world objective: the maximum (of
	profit, performance, or yield) or minimum (of loss, risk, or cost).
CO2	solve the necessary and sufficient optimality conditions for linear programming and
	demonstrate the geometrical interpretation of these conditions.
CO3	use of duality theory to solve the real-life application problems by reducing the large
	number of constraints.
CO4	justify various techniques to solve basic inventory problems.
CO5	validate various techniques to solve basic queuing theory problems.

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	PO7	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	1	3		3	3	1					2	2	3	1
CO2	2	2		2	3						1	1	1	1	2
CO3	2	2	1		1	1	2					3	2	3	2
CO4	2		1	1		3						2	3	1	2
CO5	2	1		1	2	1	1					1	3	3	2

\*High-3, Medium-2, Low-1

#### Module-I:

Linear programming problem & Simplex method: Introduction to linear programming problem, Formulation of linear programming problem, Graphical solution of linear programming problem using simplex method, Artificial variables, Solution of linear programming problem using Big-M and two-phase method

#### Module -II:

Duality in Linear Programming: Introduction, General primal-dual pair, formulating primaldual problem, Duality in simplex method, Dual simplex method.

#### Module – III:

Inventory Controls: Introduction, Inventory decision, Cost associate with inventories, Factor affecting inventory control, Economic order quantity (EOQ).

#### Module - IV:

Deterministic inventory problem with no shortages, Deterministic inventory problem with shortages, Economic order quantity (EOQ) problem with price breaks.

#### Module – V:

Elementary queuing theory: Introduction, Queuing system, Elements of queuing system, Operating characteristics of queuing system.

#### Module – VI:

Probability distribution in queuing systems, Classification of queuing models, Definition of transient and steady state.

#### Module – VII:

Steady-state solutions of Markovian queuing models: M/M/1, M/M/1 with limited waiting space, M/M/C, M/M/C with limited waiting space, M/G/1.

#### **Projects:**

- 1. Project on Inventory management system
- 2. Project on queuing theory

#### **Text Books:**

- 1. Kanti Swarup, P.K. Gupta and Man Mohan-Operations Research, S. Chand and Co. Pvt. Ltd.
- 2. Engineering Optimization Theory and Practice by Singiresu S. Rao, JOHN WILEY & SONS, INC., Fourth Edition

# **Reference Book:**

1. Mathematical Programming by N. S. Kambo, East West Press.



# CUNT2484 DESCRIPTIVE STATISTICS & DATA ANALYSIS

Subject Name	Code	Type of course	T-P-P (Credit)	Prerequisite
DESCRIPTIVE STATISTICS & DATA ANALYSIS	CUNT2484	Theory + Proj	3-0-1	Nil

#### **Objective:**

- To familiarize students with the fundamental concepts and techniques of probability theory and statistical analysis.
- To provide mathematical concepts and build strong mathematical foundations to support data science algorithms.
- To build-up a hypothetical model and validate through different techniques.

# **Learning Outcome:**

After completion of the course, students will be able to

Cos	Course outcomes
CO1	explain the concepts of sampling which can apply to business decision
CO2	apply the concepts of discrete and continuous probability distributions to make the
	prediction to the real-life application
CO3	solve the problems based on practical situations using the Binomial, Poisson and
	Normal distributions.
CO4	analyze the multivariate data through ANOVA and Co-ANOVA
CO5	develop the feature reduction techniques principle component analysis, discriminant
	analysis, cluster analysis for prediction analysis for data science algorithm

#### **Course Outcome to Program Outcome Mapping:**

COs	PO1	PO2	PO3	PO4	PO5	PO6	<b>PO7</b>	PO8	PO9	PO10	PO11	PO12	PSO1	PSO2	PSO3
CO1	3	1	3		3	3	1					2	2	3	1
CO2	2	2		2	3						1	1	1	1	2
CO3	2	2	1		1	1	2					3	2	3	2
<b>CO4</b>	2		1	1		3						2	3	1	2
CO5	2	1		1	2	1	1					1	3	3	2

\*High-3, Medium-2, Low-1

#### Module:1

Random variables and distributions functions (univariate and multivariate); Expectations and moments. Marginal and conditional distributions. Characteristic functions.

#### Module:2:

Standard discrete and continuous univariate distributions. Sampling distributions, Standard errors and asymptotic distributions, Distributions of order statistics and range.

#### Module:3

Simple non-parametric tests for one and two sample problems, Rank correlation and test for independence.

#### Module:4

Analysis of variance and covariance. Fixed, random and mixed effects models. Simple and multiple linear regression, Logistic regression.

#### Module:5

Multivariate normal distribution, Wishart distribution and their properties. Distributions of quadratic forms. Inference for parameters.

#### Module:6

Data reduction techniques: Principle component analysis, Discriminant analysis, Cluster analysis.

#### Module:7

Simple random sampling, stratified sampling and systematic sampling. Probability proportional to size sampling.

#### **Projects:**

- 1. Prepare a report on Gauss Markov models.
- 2. Prepare a report on correlation and regression analysis.

#### **Text Book:**

- 1. Irwin Miller and Marylees Miller, John E. Freund, Mathematical Statistics with Applications, 7th Ed., Pearson Education, Asia, 2006.
- 2. Sheldon Ross, Introduction to Probability Models, 9th Ed., Academic Press, Indian Reprint, 2007.
- 3. Devore, J. L.: Probability & Statistics for Engineering and the Sciences, 8th edition, Cengage Learning, 2012.

# **Reference Book:**

- 1. Milton, J. S. and Arnold J. C.: Introduction to Probability and Statistics: Principles and Applications for Engineering and the Computing Sciences, 4th edition, Tata McGraw-Hill, 2007.
- 2. Johnson, R. A., Miller: Freund's Probability and Statistics for Engineers, 8th edition, PHI, 2010.
- 3. Meyer, P.L.: Introductory Probability and Statistical Applications, 2<sup>nd</sup> edition, Addison Wesley, 1970.
- 4. Ross, S. M.: Introduction to Probability Models, 11th edition, Academic Press, 2014.